# Hoyle Fragmentation in Turbulent Molecular Clouds



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## Outline:

- The Hierarchical Gravitational Contraction (HGC) paradigm for star-forming GMCs.
- Hoyle fragmentation revisited.
  - Overcoming old objections.
  - · Approximate timescales for collapse of density fluctuations.
  - Implications.

## I. The Hierarchical Gravitational Contraction Paradigm

 Mounting observational evidence that MCs are collapsing globally and on multiple scales (0.01 – several pc), along filaments.



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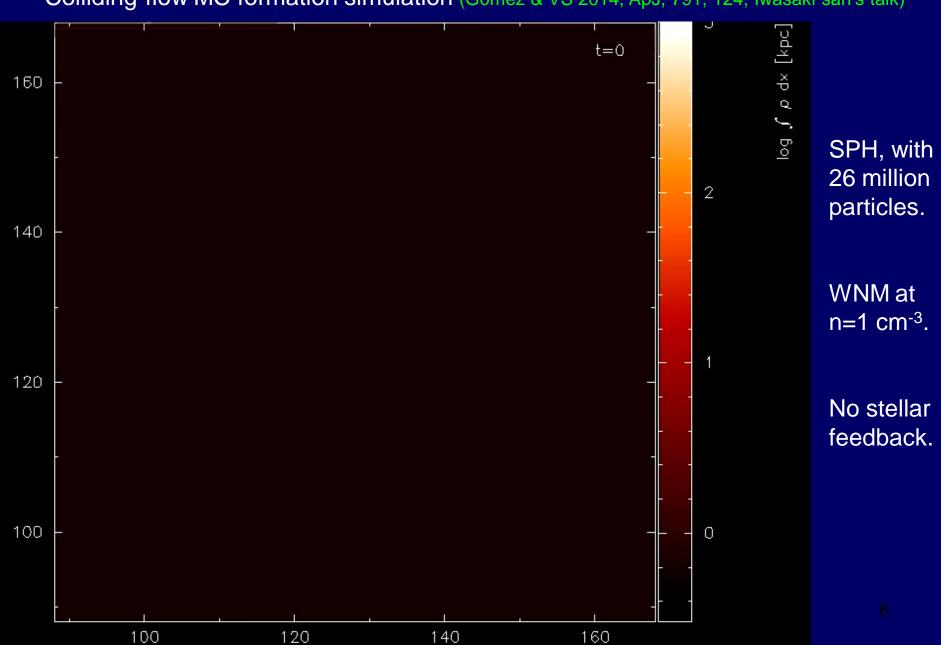
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Global collapse of molecular clouds as a formation mechanism for the most massive stars

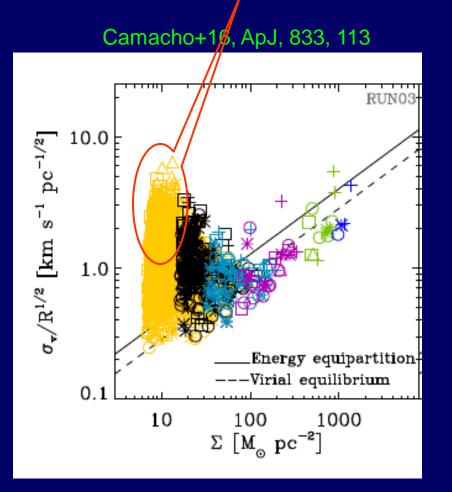
SDC13 infrared dark clouds: Longitudinally collapsing filaments?\*,\*\*,\*\*\*

N. Peretto<sup>1,2</sup>, G. A. Fuller<sup>3</sup>, Ph. André<sup>2</sup>, D. Arzoumanian<sup>4</sup>, V. M. Rivilla<sup>5</sup>, S. Bardeau<sup>6</sup>, S. Duarte Puertas<sup>7</sup>, J. P. Guzman Fernandez<sup>7</sup>, C. Lenfestey<sup>3</sup>, G.-X. Li<sup>8</sup>, F. A. Olguin<sup>9,10</sup>, B. R. Röck<sup>11,12</sup>, H. de Villiers<sup>13</sup>, and J. Williams<sup>3</sup>

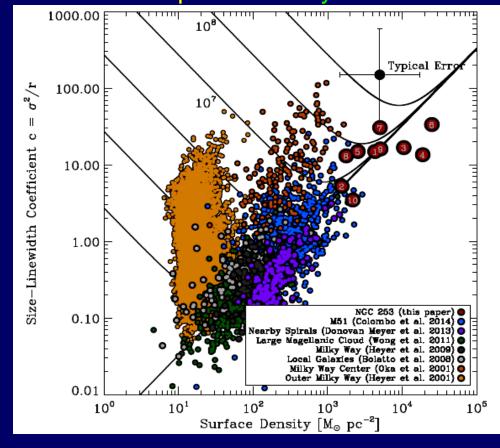
## Colliding-flow MC formation simulation (Gómez & VS 2014, ApJ, 791, 124; Iwasaki san's talk)



- Dispelling the notion that MCs are "unbound". A study of clump energy budget in simulation of turbulent assembly of MCs (Camacho+16, ApJ, 833, 113):
  - At low Σ, inertial motions dominate, but in ~1/2 of the cases, they are
     assembling the clumps (measured by <div v> in the clumps).



Compare to Leroy+15



- Turbulent velocities are largest at the largest scales.
  - → Don't act as isotropic pressure, but as *streams* (pistons, shear).
    - Tidal stretching looks like local expansion!
- Inward motions may come from gravitational instability at a larger scale (i.e., spiral arms).
- So, need to take into account weight of the CNM and CO-dark gas to determine binding.

#### The HGC scenario:

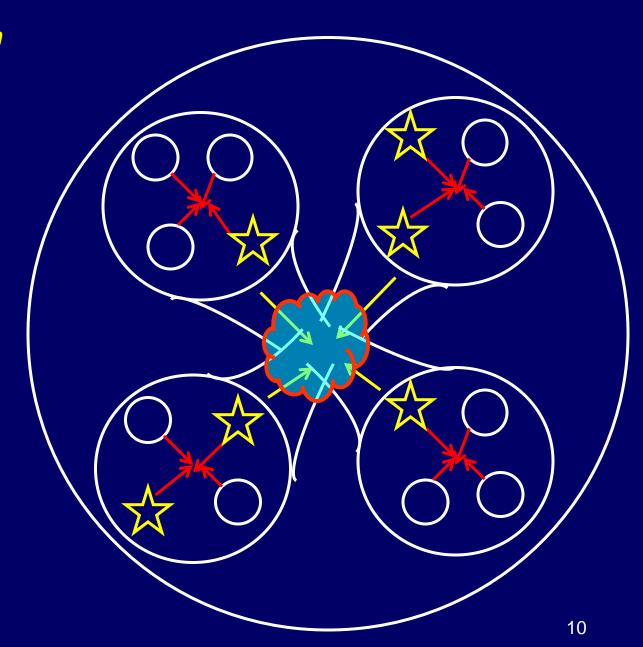
- Arose from the observed evolution of simulations of MC formation with self-gravity (VS+07, ApJ, 657, 870).
- Solar-neighborhood-type clouds form by compression-triggered phase transition WNM → CNM (Hennebelle & Perault 99; Koyama & Inutsuka 02; Heitsch+05; VS+06).
  - (Converging flows, NOT cloud-cloud collisions. Cloud "boundaries" are fake, due to tracers (Sarah's talk).)
- Jeans mass drops precipitously (x10<sup>4</sup>) by cooling/compression and cloud begins to collapse (VS+07; Gómez & VS 14).
  - Turbulence is only moderately supersonic. Not enough to prevent collapse, just a population of moderate fluctuations.
  - Clouds quickly acquire many Jeans masses.
- Collapse is *multi-scale*: small-scale collapses within and falling into larger-scale ones (VS+09, ApJ, 707, 1023).
- Massive star-forming regions consist of mergers of low-mass regions 9 occurring at late evolutionary stages.

## Gravitational contraction starts at the largest scales.

Small-scale collapses within large-scale ones develop sequentially.

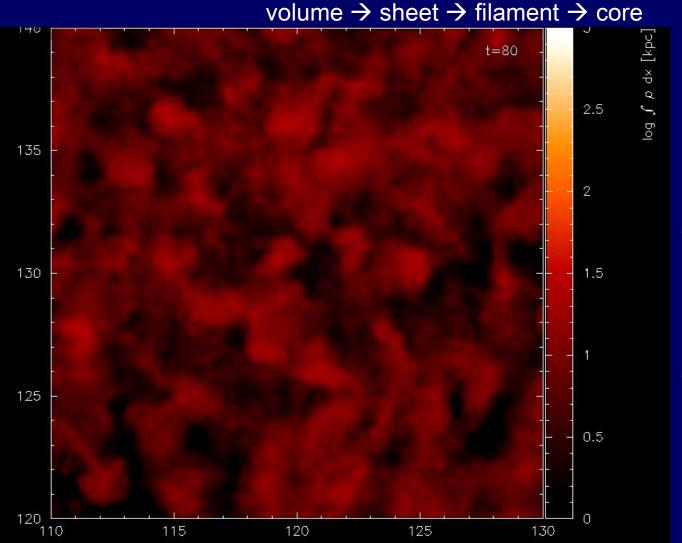
Small-scale objects terminate their collapse first because of their shorter free-fall times.

Similar to Hoyle's (1953) fragmentation, but with nonlinear fluctuations and filament formation.



## Filaments form spontaneoulsy (Gómez & VS 14, ApJ, 791, 124):

- Because the clouds contain many Jeans masses...
- ... the collapse is nearly pressureless...
- ... and proceeds first along shortest scales (Lin+65):



SPH simulation with no feedback (GV14).

Fragmentation occurs along filaments as they feed central objects.

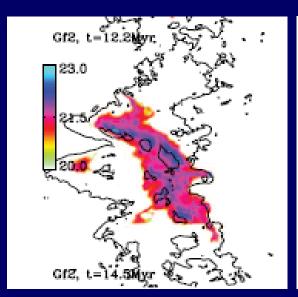
## III. Hoyle Fragmentation Revisited (VS+18, in prep.)

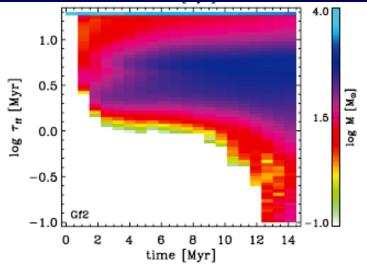
- Hoyle fragmentation (Hoyle, 1953, ApJ, 118, 513):
  - Jeans mass scales as

$$M_J \sim T^{3/2} \rho^{-1/2}$$

- In particular, for isothermal flows, M<sub>J</sub> decreases with increasing density.
  - → As an isothermal cloud contracts gravitationally, it contains ever more Jeans masses → *fragmentation*.
- The mechanism was criticized by Tohline (1980):
  - For spherical clouds just over the Jeans mass with linear fluctuations, the fastest-growing modes are the largest scales.
    - → Large-scale collapse should overwhelm small-scale one.
    - → No fragmentation

- Hoyle fragmentation in realistic MCs (VS+18, in prep.):
  - Actual MCs:
    - Are not spherical. Likely sheet-like, because their formation requires collisions of streams (Bally+87; Heiles & Troland 03; VS+06, ApJ, 643, 245).
    - Contain many Jeans masses.
      - Guszejnov+18: Number of Jeans masses determines fragmentation, not turbulent Mach number.
    - Contain *nonlinear*, turbulent density fluctuations.
      - Distribution of density fluctuations → distribution of free-fall times.





Projected cloud shape and distribution of free-fall times in a colliding-stream simulation of MC formation (Heitsch & Hartmann 2008).

- As the MC contracts, the average Jeans mass within it decreases.
  - However, must consider the Jeans mass at the density of the *typical* (rms) turbulent fluctuation, of amplitude  $\rho_{rms}/\rho_0 \sim M_s^2$ .
- Can estimate the evolution of the Jeans mass at the density of the typical density fluctuation in spherical geometry:
  - The evolution of the radius of a uniform-density collapsing sphere can be approximated by (Girichidis+14)

$$R(\tau) = R_0 (1 - \tau^2)^{a/3}$$

where  $\tau = t/t_{ff}(\rho_0)$ , and a = 1.8614 is a parameter for which the fit remains within 0.5% of the actual free-fall solution.

 From here, assuming constant mass, the mean density and the mean Jeans mass in the MC are respectively given by

$$\rho(\tau) = \rho_0 (1 - \tau^2)^{-a}$$

and

$$M_{\rm J}(\tau) = M_{\rm J}(\rho_0)(1-\tau^2)^{a/2}$$

The Jeans mass at the density of the typical fluctuation therefore evolves as

$$M_{\rm J,rms}(\tau) pprox rac{M_{\rm J}(
ho_0)}{\mathcal{M}_{\rm s}} \left(1 - au^2\right)^{a/2}$$

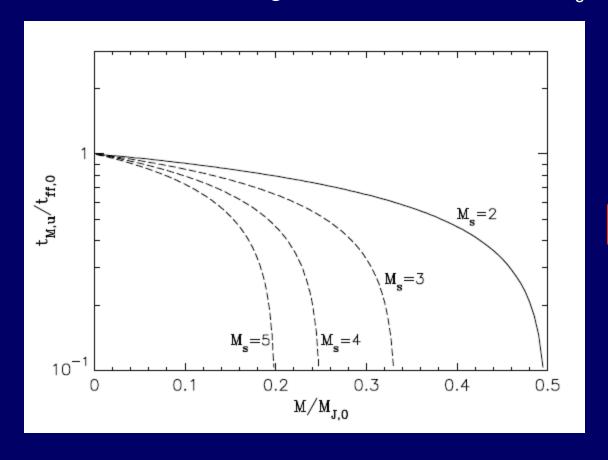
where M<sub>s</sub> is the sonic Mach number of the turbulence.

Inverting this expression, we obtain the time for mass M at the density
of the rms fluctuation to become equal to M<sub>J,rms</sub>(τ):

$$au_{
m M,u} \equiv rac{t_{
m M,u}}{t_{
m ff,0}} pprox \left[1 - \mu^{2/a}
ight]^{1/2}$$

where  $\mu \equiv \mathcal{M}_{\rm s} M/M_{\rm J}(\rho_0)$  is the fluctuation's mass normalized to the initial Jeans mass in the cloud.

 Thus, the time for mass scale M at the density of the rms turbulent fluctuation to go unstable, for various M<sub>s</sub>, is



VS+18, in prep.

Thus, sequentially smaller masses become unstable as time proceeds.

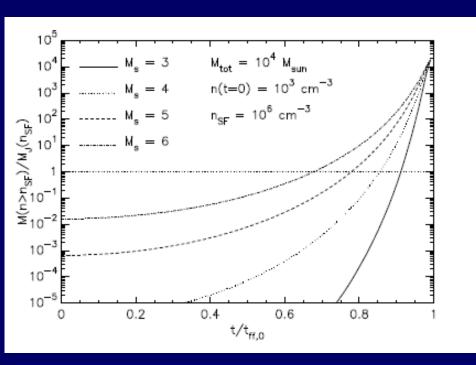
- Can also estimate the time at which the first-ever fragment collapses occur.
  - Now, consider the most extreme fluctuations, with  $t_{\rm ff}$  so small that they can be assumed to form stars instantaneously.
  - The first collapses occur when the mass above this density (given by the density PDF) equals the local Jeans mass:

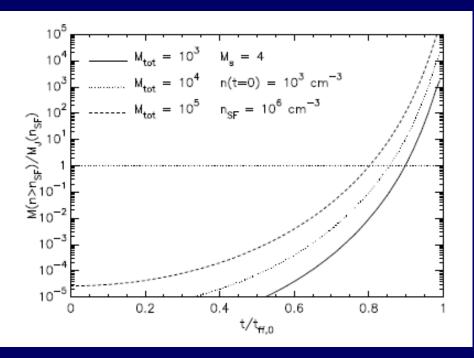
$$M(\rho \ge \rho_{SF}) = M_J(\rho_{SF})$$
Volume fraction 
$$\log n \text{ [cm}^{-3]}$$

Lognormal PDF (VS94).

As cloud collapses, mass fraction above n<sub>SF</sub> increases.

– Thus, the time for the first collapses to occur, for various  $\rm M_{\rm s}$  and various cloud masses  $\rm M_{\rm tot}$ , is





- For reasonable parameters, the first collapses typically occur between 0.7 and 0.9  $t_{\rm ff,0}$ .
  - Qualitatively consistent with simulations.

#### Implications:

- HGC is an evolutionary scenario for MCs and their SFR.
  - Contrary to stationary models for the SFR (Krumholz & McKee 05; Padoan & Nordlund 11; Hennebelle & Chabrier 11; Hopkins 12; Federrath & Klessen 12).
- Collapse starts at the large scales.
  - Smaller-scales are the "tips of the iceberg" of the large scales.
- SF accelerates (Zamora-Avilés+12, ApJ, 751, 77; Matt's talk)...
- until feedback destroys the region (Colín+13, MNRAS 435, 1701; VS+17, MNRAS, 467, 1313).
- Nonlinear turbulent fluctuations allow Hoyle-like fragmentation.
  - Sequential destabilization of progressively smaller mass scales.

#### Caveats:

- Calculations are highly idealized:
  - Based on spherical geometry.
    - Actual timescales (for sheets and filaments) are longer (Toalá+12; Pon+12).
  - Ignored accretion.
- However, illustrate time-dependence of collapse at different mass scales.

## THE END